

# **Generating AI Slop in LambdaPi**

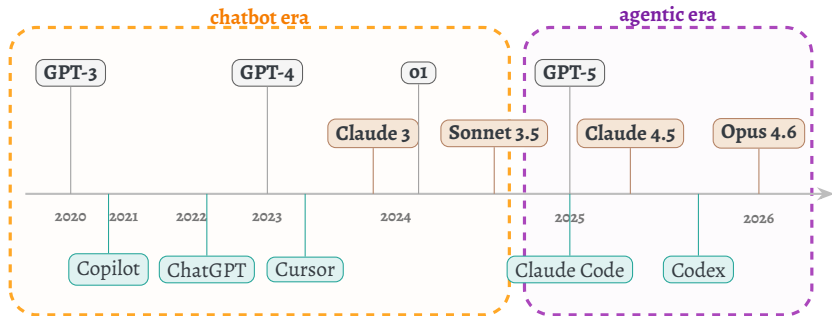
## **An Interactive Demo with Claude Code**

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# From Chatbots to Agents



# AI and Formal Math

## Lean

- LeanCopilot, LeanDojo/ReProver, Leanstral (Mistral)
- HILBERT (Apple) — 99.2% on miniF2F
- AlphaProof (DeepMind) — IMO 2024 silver

## Rocq

- CoqPilot (JetBrains), Rocq-MCP

## Isabelle

- HybridProver (59.4% miniF2F), IsaMini

All benefit from **extensive training data** — large proof corpora (Mathlib, Isabelle AFP, etc.) in the LLM pretraining mix.

# Two Ways to Extend an Agent

## **MCP** (Model Context Protocol)

- runtime ‘tool’ integration
- constrained access to databases, APIs, services

## **Agent Skills**

- literally just Markdown files
- instructions for using a CLI, where to find docs, etc.

# The LambdaPi Skill

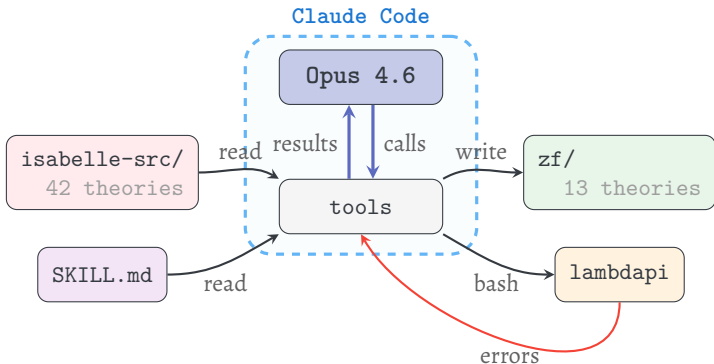
**How it was built** — written by Claude, iteratively refined

- Read `lambdapi` source, docs, and `stdlib` to draft `SKILL.md`
- Wrote 1,753 lines of test proofs — discovered 47 edge cases
- Refined: 670 → 343 lines + supporting reference files

## Final layout

- `SKILL.md` — 343 lines (loaded first)
- `STDLIB_REFERENCE.md` — 485 lines
- `CLI_REFERENCE.md` — 133 lines

# Isabelle/ZF $\rightarrow$ LambdaPi



**Goal:** formalize up to `trans_induct3`. ✓  
13/42 theories · 6,468 lines · 306 lemmas · 63 defs · ~3 hours

# Demo: Waffle



correct position    
  wrong position    
  not in word

$$\sigma = (2\ 9)(3\ 20)(4\ 15\ 6\ 8)(7\ 18)(10\ 16\ 13)(12\ 14\ 19) \quad 6 \text{ cycles, } 10 \text{ swaps}$$

# Chantal's Conjecture

**Conjecture** (Keller, 2025):

*Call a tile **free** if it is not green. If a letter appears **free exactly once**, then we can move it to its correct position and **remain optimal**.*

**Let's formalize this!**

Claude Code + LambdaPi Skill

